

# BACHELOR OF ECONOMICS

# EES 405: NON-PARAMETRIC AND SEMI PARAMETRIC STATISTICS

#### DATE: 9/12/2019

TIME: 2.00-4.00 PM

#### **INSTRUCTIONS:**

- (i) Answer question one (Compulsory) and any other two questions
- (ii) Show your working clearly
- (iii) Where significance level is not provided, use 5%.
- (iv)  $H_{critical}=5.991$

# QUESTION ONE (COMPULSORY)(30 MARKS)

a)	Explain the differences between parametric, non-param	etric and semi parametric in terms of
	estimation and type of data	(6 marks)

- b) State three examples of non-parametric tests (3 marks)
- c) Explain main assumptions that have to be fulfilled before applying parametric tests

(5 marks)

- d) Explain two types of decision errors in non-parametric statistics (4 marks)
- e) The weights of leaves produced by plants from the same original source after an experiment comparing two artificial day lengths I and II were as follows;

Ι	172	51	123	69	82	135	133	112	116	142	108	71		
Π	190	153	124	175	128	130	146	106	67	93	158	168	101	191

Test the hypothesis of equal medians at  $\alpha = 0.02$  level of significance and

$$\propto =0.1$$
 (10 marks)

f) Clearly explain situations when spearman's rank correlation coefficient is applied (2 marks)

#### **QUESTION TWO (20 MARKS)**

- a) What do you understand by the term 'level of significance?' (2 marks)
- b) Explain your understanding of Mann-Whitney U-test in terms of the characteristics of the sample and observations (3 marks)
- c) Explain three conditions under which non-parametric test may be applied (3 marks)
- d) Suppose you are given the following observations of an individual's income (Y) and corresponding purchase of commodity (X).

Income (US\$) (Y) 2556 2307 2348 2533 2613 2721 3075 3181 Commodity (X) 1301 1332 1449 1272 1205 897 1009 1264 (units)

Calculate the Spearman's rank correlation coefficient between average income (Y) and consumption levels of commodity (X) and test whether significant negative Spearman's rank correlation exists. (10 marks)

e) Explain scenarios when a parameter enjoys 'statistical power' (2 marks)

#### **QUESTION THREE (20 MARKS)**

- Explain three common levels of significance used in for either parametric, non-parametric a) and semi parametric hypothesis testing (3 marks) Why do you think Wilcoxon signed rank test statistic is considered to be powerful than the b) ordinary sign test? (2 marks) Explain the meaning of the term 'Parameter' as applied in in Non-parametric and Semic) Parametric statistics (2 marks) d) Give three examples of parametric tests (3 marks) e) Performance of Statistics and Economics units in Machakos University is observed and
- recorded out of 20. Do the data present sufficient evidence to indicate a difference in the performance level?

Group	1	2	3	4	5	6	7	8	9	10
Statistics (A)	12.1	14.3	13.5	15.1	13.9	11.7	14.8	14.2	12.9	14
Economics (B)	14.9	13.7	16.7	15	13.1	12.9	15.2	13.7	14.4	15.3

Test the claim at  $\alpha = 0.05$  and 0.10 levels

(10 marks)

# **QUESTION FOUR (20 MARKS)**

- a) It is suggested that it is **NOT** advisable to apply parametric tests to the nominal and ordinal data. Explain two exceptions (2 marks)
- b) Write clearly the steps of performing the Wilcoxon Signed Rank Test (8 marks)
- c) Explain the meaning of the uniformly most powerful test as applied in statistics (2 marks)
- d) The following observations were randomly obtained as a sample data for eight classes. The median class is claimed to be 4.

2.3 4.5 3.4 7.8 3.4 6.6 6.1 9.5

Using appropriate test, ascertain the claim at the  $\alpha = 0.05$  level of significance (8 marks)

#### **QUESTION FIVE (20 MARKS)**

- a) Using appropriate figure, explain the difference between directional and non-directional hypothesis. (2 marks)
- b) Discuss four main advantages of non-parametric tests over parametric tests (8 marks)
- c) A quality control chart has been maintained for the weights of paint cans taken from a conveyor belt at a fixed point in a production line. Sixteen (16) weights obtained today, in order of time, are as follows;

68.2 71.6 69.3 71.6 70.4 65.0 63.6 64.7 65.3 64.2 67.6 68.6 66.8 68.9 66.8 70.1

d) Use the run test, at approximately a 0.01 level, to determine whether the weights of the paint cans on the conveyor belt deviate from randomness. (10 marks)